

**IMPORTANT FIRST STEPS:**

1. Form a group of 2 students.
2. Clearly put your names and IDs on 1 copy of this worksheet.
3. Be sure to turn this exercise in at the end of class.
4. Do not attempt to prove the inductive step until you have completed all other steps for each question.

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**Mathematical Induction**

1. Using mathematical induction, prove the following:

$$1^2+2^2+3^2+\dots+n^2 = n(n+1)(2n+1) / 6$$

S(n):  $1^2+2^2+3^2+\dots+n^2 = n(n+1)(2n+1) / 6$

Claim:  $\forall n > 0, S(n)$  holds.

Base Case, express and prove:

Inductive Hypothesis: Assume S(n), that is  $1^2+2^2+3^2+\dots+n^2 = n(n+1)(2n+1) / 6$

What is to be proven using the Inductive Step? Write this out explicitly:

Prove S(n+1) is also true:  $1^2+2^2+3^2+\dots+(n+1)^2 = (n+1)((n+1) + 1)(2(n+1) + 1) / 6$

Now, prove the Inductive Step:

Statement that you've proven your claim:

QED.

2. Using mathematical induction, prove the following:

$$1^3 + 2^3 + 3^3 + \dots + n^3 = n^2(n+1)^2 / 4$$

S(n):

Claim:

Base Case, express and prove:

Inductive Hypothesis:

What is to be proven using the Inductive Step? Write this out explicitly:

Now, prove the Inductive Step:

Statement that you've proven your claim:

QED.

3. Using mathematical induction, prove that the distributed property of OR can be extended to a disjunction with a conjunction of  $n$  sentences. ie.

$$(a \vee (b \wedge c \wedge \dots \wedge n)) = (a \vee b) \wedge (a \vee c) \wedge \dots \wedge (a \vee n)$$

S(n):

Claim:

Base Case, express and prove:

Inductive Hypothesis:

What is to be proven using the Inductive Step? Write this out explicitly:

Now, prove the Inductive Step:

Statement that you've proven your claim:

QED.

4. Prove that the sum of the interior angles of a convex polygon of  $n$  sides is  $(n-2) * 180$  degrees.

$S(n)$ :

Claim:

Base Case, express and prove:

Inductive Hypothesis:

What is to be proven using the Inductive Step? Write this out explicitly:

Now, prove the Inductive Step:

Statement that you've proven your claim:

QED.